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2. \_\_\_\_\_ “ 25 ” \_\_\_\_\_ 2021 . \_\_\_\_\_ 169  
\_\_\_\_\_ 13 \_\_\_\_\_ 2020 .

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2		13.11.21-18.11.21	
3		19.11.21-22.11.21	
4		23.11.21-29.11.21	
5		30.11.21-03.12.21	
6		04.12.21-07.12.21	
7		08.12.21-09.12.21	
8		10.12.21-11.12.21	

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## ABSTRACT

Master's thesis: 86 pages, 12 figures, 17 tables, XX appendices, 16 sources.

IMAGE, DIGITAL WATERMARK, STEGANOGRAPHY, COPYRIGHT.

The major goal of this thesis is to compare the existing algorithms, identify their advantages and disadvantages and justify the choice of an effective method of applying DW.

Indicators such as algorithm resilience to attacks, runtime, and stego bandwidth capacity were selected as comparison criteria.

The objectives of the study are a detailed study of the subject area, the existing algorithms for generating and embedding DW in the image, creating a software package that implements the most popular algorithms, a detailed comparison of implemented algorithms for each criterion. The results will be presented in the form of tables and graphs and for each of the algorithms will determine its optimal scope.

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1.1				11
1.2	.....			12
1.3	.....			13
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EBCOT —

LSB — Least Significant Bit

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Digimarc

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Adobe Photoshop,

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Digimarc

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[1].

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ManART, Tokishi).

[2].

### 1.3

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Digimarc.

Digimarc,

URL-

URL,

[3].

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1.4

( Epson )

[1].





( ) , [4].

2.2

$W^*, K^*, I^*, B^*$  ,  
 $F : I^* \times K^* \times B^* \rightarrow W^*$  ,  $W = F(I, K, B)$  ,  $W, K, I, B$  -  
 $F$  ,  
 $F(I, K, B) \approx F(I + \nu, K, B)$   
 $F$  :  
 $F = T \circ G$  ,  $G : K^* \times B^* \rightarrow C^*$   $T : C^* \times I^* \rightarrow W^*$  ,

$$\begin{aligned}
 & T \quad C^* , \\
 W^* . & \\
 & T \quad , \quad I_0 , \\
 & I_W \\
 I_W & : T(C, I_0) = T(C, I_W) = T(C, I'_W),
 \end{aligned}$$

$$\begin{aligned}
 & W(i, j) \quad I_0(i, j) \\
 & : \\
 v : I^* \times W^* \times L^* \rightarrow I_W^* , & I_W(i, j) = I_0(i, j) \oplus L(i, j)W(i, j)p(i, j), \quad L(i, j) -
 \end{aligned}$$

$$\begin{aligned}
 & , \\
 & ; p(i, j) - \\
 \oplus &
 \end{aligned}$$

[4].

( , ). « » ( )  
 D.

$$\begin{aligned}
 D : I_W^* \times K^* \rightarrow \{0,1\}, D(I_W, W) = \\
 D(I_W, F(I_W, K)) = \begin{cases} 1, & W \\ 0, & W \end{cases} \quad (2.1)
 \end{aligned}$$

$$1, - \quad 1. \quad I_W = I_0 + W , \quad F(I_0, K) = W .$$

$$I_w * W = (I_0 + W) * W = I_0 * W + W * W. \quad W$$

$$\pm 1, \quad I_0 * W, \quad W * W, \quad I_w * W$$

$$W * W.$$

$$,$$

$$W * W \quad (\ll \quad \gg)$$

$$(\ll \quad \gg).$$

$$,$$

$$:$$

$$u = \frac{I_0 I_w}{\|I_0\| \|I_w\|} - \quad (2.2)$$

$$u = N - \sum_{i=1}^N i_0 i_w - \quad [4] \quad (2.3)$$

3.

3.1

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I,

$\Delta I$

[6].

( )

[4].

3.2.

3.2.1 BMP (Bit MaP)

BMP

BMP

RGB.

–  $2^{16} - 1$  . RGB-

,

256-

– 0  $2^8-1$ .

–  $2^{24}$  ( TrueColor).

4, 8, 16

[5].

BMP

(TrueColor)

BMP

.BMP; . ;

.RLE.

### 3.2.2 PNG (Portable Network Graphics)

PNG

« » « »

PNG

PNG

RGB.

–  $2^{32} - 1$  . RGB-

256- (

256 ),

TrueColor.

PNG

16

2<sup>48</sup>

LZ77,

[5].

PNG

. PNG

« »

JPEG

BMP,

PNG

( , ),

1

PNG

.PNG.

### 3.2.3 TIFF (Tagged Image File Format)

TIFF

TIFF

TIFF

70

TIFF,

TIFF

TIFF

. TIFF

: RGB,

LAB, CMYK

:

(

)  $2^{32}$ . RGB  
 ,  
 - 0  $2^8 - 1$ .  
 -  $2^{24}$  ( TrueColor).  
 1, 2, 4, 8, 16, 32 .  
 ( - RLE LZW,  
 - Deflate, JPEG ) [5]. TIFF

/  
 ,  
 , -  
 .  
 . TIFF . TIF; .TIFF.

### 3.2.4 JPEG (Joint Photographic Expert Group)

, TIFF,  
 ,  
 TIFF. JPEG  
 RGB. - 216 - 1  
 . RGB-  
 - 0  $2^8-1$ . - $2^{24}$  ( TrueColor).  
 24 /  
 , ( 28  
 ) [5].

JPEG

JPEG

JPEG

JPEG-

JPEG

.JPG; .JPEG; .JFIF.

2000.

JPEG-2000

JPEG – JPEG-

«

EBCOT

» (EBCOT).

Windows

### 3.3

#### 3.3.1

(LSB – Least Significant Bit) –

1/8

, ( , ) [7].

, [7].

, « ».

, ( .),

3.3.2

(M. Kutter), (F. Jordan) (F. Bossen) [8]

RGB-

$M_i$  - ,  $= \{R, G, B\}$  - ,  $p(x, y)$  - ,

$M_i$

$$\}_{x,y} = 0,2989 * R_{x,y} + 0,58662 * G_{x,y} + 0,11448 * B_{x,y} :$$

$$B_{x,y} = \begin{cases} B_{x,y} - \hat{*} \}_{x,y}, & m_i = 0 \\ B_{x,y} + \hat{*} \}_{x,y}, & m_i = 1 \end{cases} = B_{x,y} + (2 * m_i - 1) * \hat{*} \}_{x,y} , \quad (3.1)$$

" " 7x7.  $\hat{B}_{x,y}^*$  :

$$\hat{B}_{x,y}^* = \frac{1}{4 * \dagger} \left[ \sum_{i=-\dagger}^{+\dagger} B_{x+i,y}^* + \sum_{j=-\dagger}^{+\dagger} B_{x,y+j}^* - 2 * B_{x,y}^* \right], \quad (3.2)$$

$\dagger = 3$  ( 7x7  $\dagger = 3$ ).  
 $(B_{x,y}^* \hat{B}_{x,y}^* p(x,y))$   
 $u : u < 0, M_i = 0 ; u > 0,$   
 $M_i = 1.$

( $\hat{u}$ ,  $\hat{b}$ ).  
 $\hat{u}$ ,  $\hat{b}$ .

$$\hat{u} = \hat{b}^{-1} \sum_{i=1}^{\hat{b}} [B_{x,y}^* - \hat{B}_{x,y}^*] . \tag{3.3}$$

$\hat{u}$ .

$$\hat{u} = 0,05 \quad \hat{b} = 200.$$

$\hat{b}$ .

### 3.3.3 PatchWork

Patchwork [9].

(1, 5),

(~10000)

$a_i$ ,  $b_i$ ,

$$S_n = \sum_{i=1}^n [(a_i + u) - (b_i - u)] = 2un + \sum_{i=1}^n (a_i - b_i) . \tag{3.4}$$

$$\sum_{i=1}^n (a_i - b_i)$$

$n$ .

$S_n$

$2u$ .

$S_n$

[4].

( patches, ).

JPEG,

Patchwork

20000

[4].

3.3.4

)

(

JPEG

JPEG2000 –

[4].

« » [4].

( . Koch)

(J. Zhao) [10].

: (3.5) –

, (3.6) –

$$\Omega(\hat{\epsilon}, \epsilon) = \frac{(\hat{\epsilon}) * (\epsilon)}{\sqrt{2N}} * \sum_{x=0}^{N-1} \sum_{y=0}^{N-1} C(x, y) * \cos\left[\frac{f * \hat{\epsilon} * (2x+1)}{2N}\right] * \cos\left[\frac{f * \epsilon * (2y+1)}{2N}\right], \quad (3.5)$$

$$S(x, y) = \frac{1}{\sqrt{2N}} * \sum_{\hat{\epsilon}=0}^{N-1} \sum_{\epsilon=0}^{N-1} (\hat{\epsilon}) * (\epsilon) * \Omega(\hat{\epsilon}, \epsilon) * \cos\left[\frac{f * \hat{\epsilon} * (2x+1)}{2N}\right] * \cos\left[\frac{f * \epsilon * (2y+1)}{2N}\right] \quad (3.6)$$

8x8

(3.5),

8x8

$$\Omega_b(\hat{\epsilon}, \epsilon) \quad b - \quad , a (\hat{\epsilon}, \epsilon) -$$

[10].

$$: (\hat{\epsilon}_1, \epsilon_1) \quad (\hat{\epsilon}_2, \epsilon_2).$$

$C_b$

$b.$

"0"

"1"

$$|\Omega_b(\hat{\epsilon}_1, \epsilon_1)| - |\Omega_b(\hat{\epsilon}_2, \epsilon_2)| > P, \quad m_b = 0; \tag{3.7}$$

$$|\Omega_b(\hat{\epsilon}_1, \epsilon_1)| - |\Omega_b(\hat{\epsilon}_2, \epsilon_2)| < -P, \quad m_b = 1; \tag{3.8}$$

(3.7-3.8),

,  
:

$$m_b^* = 0, \quad |\Omega_b^*(\hat{\epsilon}_1, \epsilon_1)| > |\Omega_b^*(\hat{\epsilon}_2, \epsilon_2)|; \quad (3.9)$$

$$m_b^* = 1, \quad |\Omega_b^*(\hat{\epsilon}_1, \epsilon_1)| < |\Omega_b^*(\hat{\epsilon}_2, \epsilon_2)|; \quad (3.10)$$

,

.

### 3.3.5 (Barni)

$w_i \in \{-1, 1\}$ .

$M \quad N, \quad :$

$$i = 0, \dots, 3 \times \frac{M}{2} \times \frac{N}{2} - 1 \quad (3.11)$$

$$(l = 4)$$

-

-6.

.

(LH, HL, HH),

:

$$\begin{aligned} f'(m, n) &= f(m, n) + \Gamma S(m, n) w_i, \\ S(m, n) &= {}_n(l, \dagger) \times A(l, m, n) \times \Xi(l, m, n). \end{aligned} \quad (3.12)$$

$u(l, \dagger)$

:

$$u(l, \dagger) = \begin{cases} \sqrt{2}, \dagger \in HH \\ 1, \dagger \notin HH \end{cases} \times \begin{cases} 1.00 & l=1 \\ 0.32 & l=2 \\ 0.16 & l=3 \\ 0.1 & l=4 \end{cases}, \quad (3.13)$$

$A(l, m, n)$ :

$$A(l, m, n) = \frac{1}{256} f_4^{LL} \left( \frac{m}{2^{4l}} \times \frac{n}{2^{4l}} \right), \quad (3.14)$$

$\Xi(n, m, l)$  [4].

$w_i$  - ( )

3.3.6 ( - )

(PC SS Spread-Spectrum)

, [7].

( )

(JR Smith)  
 ( . . . Comiskey) [11]. :

$$m_i \{_i X \times Y, (1 \ 0), +1 \ -1;$$

$$E(x, y) = \sum_i m_i * \{_i(x, y). \tag{3.15}$$

$$S(x, y) = ( , y) + ( , ), \quad x = 1..X, y = 1..Y .$$

$$\langle \{_i, \{_j \rangle = \sum_{x,y} \{_i(x, y) * \{_j(x, y) = n_{\zeta} * G^2 * u_{i,j}, \tag{3.16}$$

$$n_{\zeta} - ; G^2 - c$$

$$u_{i,j} = \begin{cases} 1, & i = j \\ 0, & i \neq j \end{cases} . \tag{3.17}$$

$$\{_i : \langle \tilde{N}, \{_i \rangle = 0, \forall i .$$

$$\langle \tilde{N}, \{i\} \rangle = \Delta \approx 0, \quad G^2$$

$G$  ( ),

$$\{i\} \pm 1 \quad [11]. \quad \{i\}$$

$(x, y) - \{i\}$

$(x, y) -$

$(n_\zeta)$ .

$$P = \sum_{x,y} \left( \sum_i G * m_i * \{i(x, y)\} \right)^2 = \sum_i \sum_{x,y} (G * m_i * \{i(x, y)\})^2 = \quad (3.18)$$

$$G^2 * X * Y = N_\zeta * n_\zeta * G^2.$$

S

$$\{i\} : \dagger_i = \langle S^*, \{i\} \rangle = m_i * n_\zeta * G^2.$$

$m_i$

:

$$m_i^* = \text{sign}(t_i) = \begin{cases} -1 & t_i < 0; \\ 1, & t_i > 0; \\ ? & t_i = 0, \end{cases} \quad , \quad G^2 \gg 0. \quad (3.19)$$

$$t_i = 0$$

3.3.7

[12]

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( -6, ),

JBIG (Joint Binary Image Group).

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( )- ( ) - .  
« »  
: , - [4].

3.3.8

[13]

 $n$ 

-

 $n-$  $v_i$ 

,

 $w_i :$ 

$$v' = v + rC(w_i) \quad (3.20)$$

,  $n = 4$ 

$$e = \frac{v^* - v}{r} \quad (3.21)$$

$$w_i = \min_{w_i} \|C(w_i - e)\| \quad (3.22)$$

[13].

3.3.9

« » , 15 , 16 4 4, 15 . ( ) .

$$W_j = r \frac{D_j - \bar{D}_j}{\max(D_j - \bar{D}_j)}, \tag{3.23}$$

$\bar{D}$  - D.  $R_j$

$$R_j' = W_j + \text{int}\left(\frac{R_j}{s}\right)s + \frac{s}{2} \tag{3.24}$$

$s$  ,  $D_j$   $W_j$  .  $R_j$

$$\widehat{W}_j' = R_j - \text{int}\left(\frac{R_j}{s}\right)s - \frac{s}{2} \tag{3.25}$$

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RGB-

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(Average Absolute Difference):

$$AD = \frac{1}{XY} \sum_{x,y} |C_{x,y} - S_{x,y}| \quad (4.1)$$

(Normalized Average Absolute Difference):

$$NAD = \frac{\sum_{x,y} |C_{x,y} - S_{x,y}|}{\sum_{x,y} |C_{x,y}|} \quad (4.2)$$

" / " (Signal to Noise Ratio):

$$SNR = \frac{\sum_{x,y} (C_{x,y})^2}{\sum_{x,y} (C_{x,y} - S_{x,y})^2} \quad (4.3)$$

" / " (Peak Signal to Noise Ratio):

$$PSNR = XY * \frac{\max_{x,y} (C_{x,y})^2}{\sum_{x,y} (C_{x,y} - S_{x,y})^2} \quad (4.4)$$

(Image Fidelity)

$$IF = 1 - \frac{\sum_{x,y} (C_{x,y} - S_{x,y})^2}{\sum_{x,y} (C_{x,y})^2} \quad (4.5)$$

. 4.1-4.7



4.1 –

(Nure.jpg)



4.2 –

(Tulips.jpg)



4.3 –

(photo.jpg)



4.4 –

(Lena.bmp)



4.5 –

(city.png)



4.6 – ,

(Logo.png)



4.7 – , TIFF (sky.tiff)

”, ASCII (8 ).

– 25 , – 200 .

Nure.jpg, -

1024x768 . ,

( – ). .

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4.1.

4.1 –

Nure.jpg

	AD	NAD	SNR	PSNR	IF
LSB	0,480371	0,003992	34762,4	121153	99,997%
Kutter	4,14126	0,034373	27,0141	87,912	96,556%
Cox	0,938733	0,009512	23456,9	66099,6	99,995%
Smith	0,873914	0,009255	18567,1	50406,7	99,994%

LSB. ,  
 " - "  
 , ( )  
 , , )  
 , LSB,  
 Kox Smith. Kox ,  
 JPEG.  
 ( ),  
 Smith,  
 Kutter.  
 ,  
 ( )  
 ,  
 ),  
 ~ 0,15.  
 « »,  
 250 (‡ = 250), “ -  
 ”. , 96% ,

( $\alpha = 0,05$ ),

Tulips.jpg,

1024x768

4.2.

4.2 –

Tulips.jpg

	AD	NAD	SNR	PSNR	IF
LSB	0,50	0,0072	30098	130021	99,99%
Kutter	0,64	0,0095	96,96	404,761	98,96%
Cox	0,61	0,0090	24078,8	104635	99,99%
Smith	0,93	0,0140	9989,6	44986,9	99,99%

Kox.

(P=2).

P

Smith,

Kox

Kutter.

5 (

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50.

" - "

99%).

photo.jpg

1600×1200

### 4.3.

4.3 –

photo.jpg

	AD	NAD	SNR	PSNR	IF
LSB	0,500186	0,005061	29710,2	130002	99,9966%
Kutter	0,207647	0,002101	2441,74	10684,2	99,959%
Cox	0,994167	0,01006	14947,8	65406,5	99,9933%
Smith	0,871591	0,00882	13141,3	57501,7	99,9924%

Kutter,

250.

Cox Smith.

JPEG.

Lena.bmp,

BMP ( )

512x512. BMP

4.4.

4.4 –

Lena.bmp

	AD	NAD	SNR	PSNR	IF
LSB	0,50032	0,004746	24526,8	101185	99,9959%
Kutter	0,9866	0,00936	1723,36	7109,71	99,942%
Cox	18,2043	0,1727	35,8981	148,097	97,2143%
Smith	0,859631	0,008155	11852,6	48897,7	99,9916%

LSB

Smith.

Kutter.

Kox,

Kox

City

PNG

1200x801

4.5.

4.5 –

City.png

	AD	NAD	SNR	PSNR	IF
LSB	0,499378	0,007036	13332,3	88309,9	99,9925%
Kutter	0,188796	0,00266	6548,79	43377,6	99,9847%
Cox	27,9807	0,394223	8,25231	54,6611	87,8821%
Smith	0,827543	0,011659	7248,92	48015,1	99,9862%

LSB, Kutter Smith

Kutter

(

).

-

Kox

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-

Logo

PNG.

(

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»).

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468x508.

4.6.

4.6 –

Logo.png

	AD	NAD	SNR	PSNR	IF
LSB	0,499449	0,002513	95744,2	130193	99,999%
Kutter	10,9237	0,054136	19,6862	26,6672	94,9203%
Cox	0,883	0,004376	54150,1	73352,4	99,9982%
Smith	0,996071	0,004936	27691,8	37511,7	99,9964%

LSB, Kox Smith

Kox

Kox

P

2

Kutter

170,

Sky

TIFF

650x487

4.7.

4.8 –

MilkyWay.tiff

	AD	NAD	SNR	PSNR	IF
LSB	0,499346	0,008378	14982,6	130220	99,9933%
Kutter	0,383127	0,006428	885,517	7696,4	99,8871%
Cox	0,982208	0,016479	7609,06	66133,5	99,9869%
Smith	18,6553	0,312991	14,4246	125,37	93,0674%

, , LSB Kox.  
 ‡ Kutter 180.

Smith.

 $K_G$  20 ,

Smith

4 , -3 , -2,  
 -1 -0 .

4.8.

4.8 –

	Nure	Tulips	photo	Lena	city	Logo	sky	
LSB	4	4	4	4	4	4	4	28
Kutter	1	1	1	2	2	0	2	9

4.8

Kox	3	3	3	0	0	3	3	15
Smith	2	2	2	3	3	2	0	14

LSB.

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Kox,

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,

(

-JPEG).

Smith,

,

Kutter.

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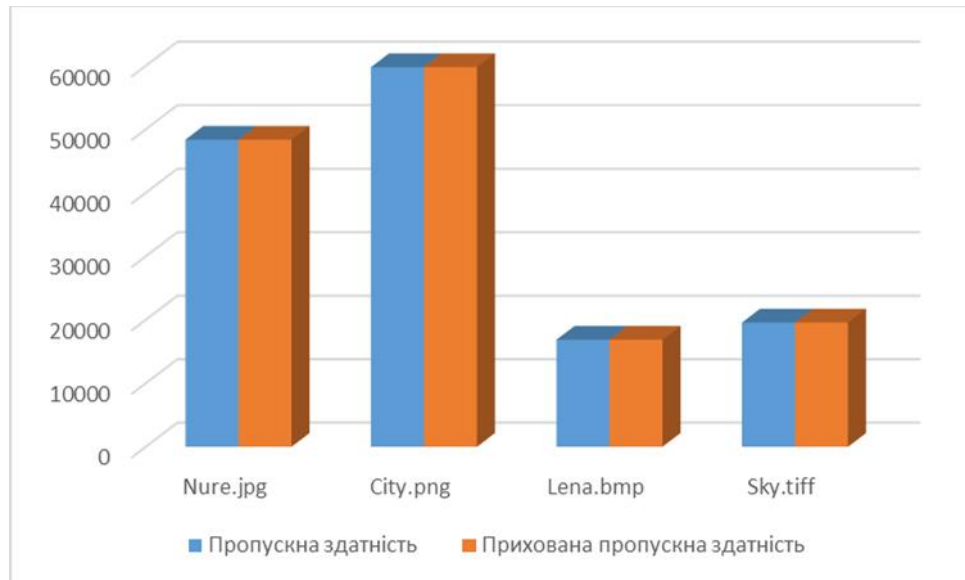
ASCII (1 =8 ),

LSB (

)  $C = M * N / 16$ ,  $M \quad N -$

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.4.8.



4.8 –

LSB

$$M * N / 8.$$

Nure.jpg

$$\ddagger = 200; \hat{=} = 0,05$$

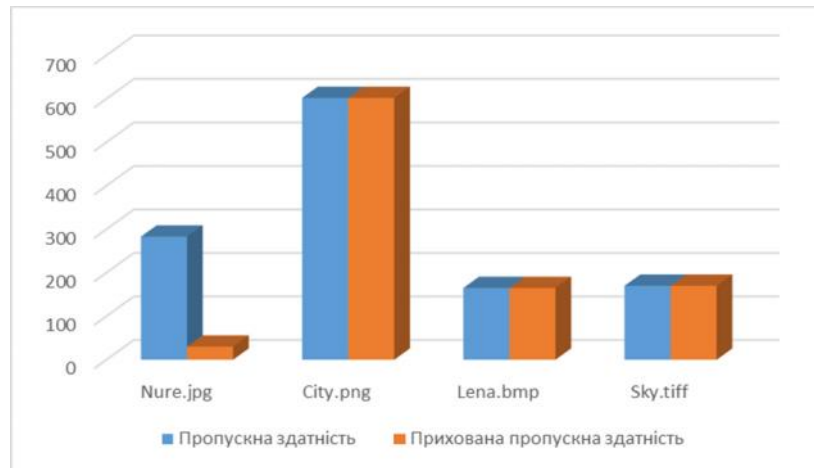
$$\text{Lena.bmp } \ddagger = 200; \hat{=} = 0,05;$$

$$\text{City.png } \ddagger = 200; \hat{=} = 0,05;$$

Sky.tiff

$$\ddagger = 180; \hat{=} = 0,05.$$

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4.9 –

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 $C$  $M * N / 512.$ 

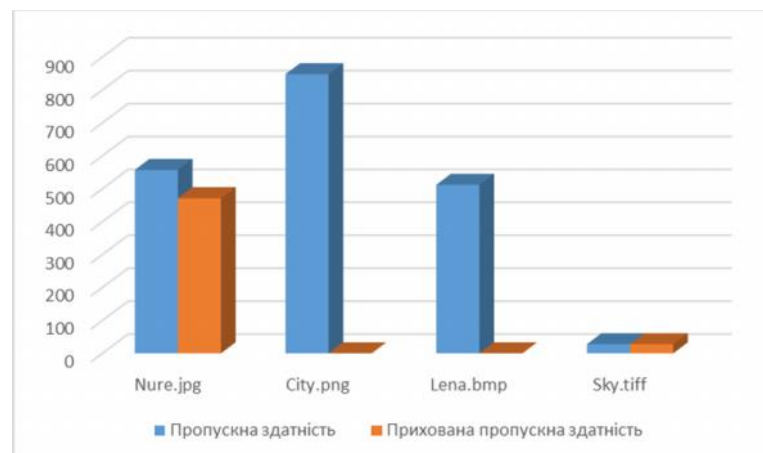
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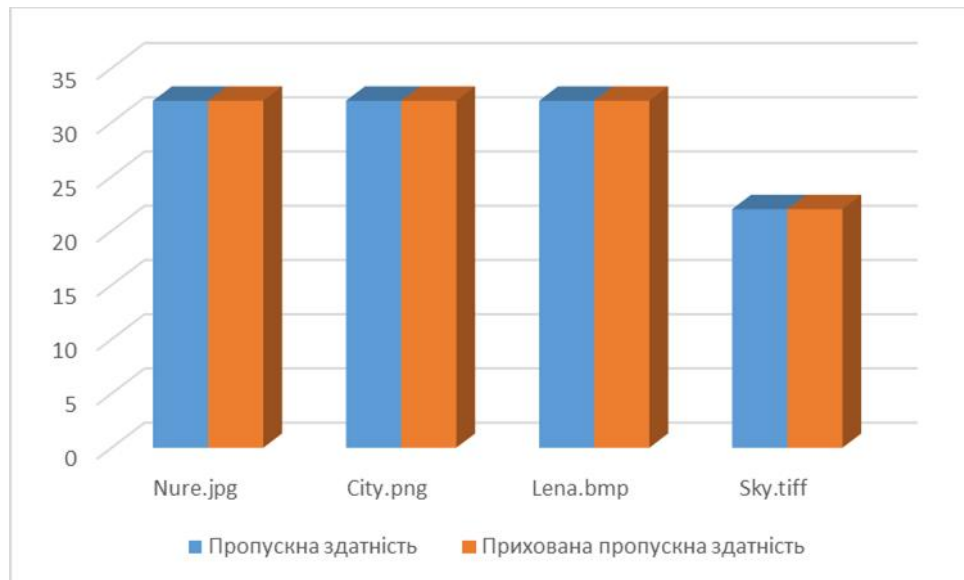


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$$M * N / 8.$$

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$$W = F(S_0, W),$$

$S_0$ .

$$S_0 + W, S_1 + W, \dots, S_N + W .$$

$NW$ ,

$N$

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$$p_1 \quad p_2 = 1 - p_1 .$$

$$p_1 W_1 + (1 - p_1) W_2 .$$

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Nure.jpg.

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Nure.jpg

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	-	-	+	+
	-	-	+	+
	-	+	+	+
	-	+	+	+
	-	+	+	+
	-	-	+	+
	+	+	-	-
	-	+	-	-
	+	+	+	-
	-	+	-	-
JPEG	-	-	+	+
0,7				
JPEG	-	-	+	+
0,5				

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Lena.bmp.

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Lena.bmp

	LSB	Kutter	Kox	Smith
	-	-	-	-
	-	-	+	+
	-	+	+	+
	-	+	+	+
	-	+	+	+
	-	-	+	+
	-	+	-	-
	-	+	-	-
	+	+	+	-
	-	+	-	-
JPEG	-	-	+	+
0,7				
JPEG	-	-	+	+
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City.png.

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City.png

	LSB	Kutter	Kox	Smith
	-	-	-	-
	-	-	+	+
	-	+	+	+
	-	+	+	+
	-	+	+	+
	-	+	+	+
	-	-	+	+
	+	+	-	-
	-	+	-	-
	+	+	+	-
	-	+	-	-

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JPEG 0,7	-	-	+	+
JPEG 0,5	-	-	+	+

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4.12

Sky.tiff.

4.12 –

City.png

	LSB	Kutter	Kox	Smith
	-	-	-	-
	-	-	+	+
	-	+	+	+
	-	+	+	+
	-	+	+	+
	-	-	+	+
	-	+	-	-
	-	+	-	-

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	+	+	+	-
	-	+	-	-
JPEG 0,7	-	-	+	+
JPEG 0,5	-	-	+	+

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7 : Nure.jpg ( -  
 ), Tulips.jpg ( - ), photo.jpg ( -  
 ), Lena.bmp ( -  
 ), city.png ( - ), logo.png ( -  
 ), Sky.tiff ( -  
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4.13

4.13 –

	Intel Core i5 660 3.33 GHz
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clock time.

4.14 – 4.17.

4.14 –

	+		+	
Nure.jpg	0,427	1,362	1,036	2,825
Tulips.jpg	0,423	1,312	1,033	2,768
Photo.jpg	0,984	3,254	2,594	6,832
Lena.bmp	0,151	0,467	0,362	0,98
City.png	0,517	1,75	1,29	3,557
Logo.png	0,137	0,508	0,341	0,986
MilkyWay.tiff	0,185	0,546	0,415	1,146

4.15 –

	+		+	
Nure.jpg	0,002	0,477	0,375	0,854
Tulips.jpg	0,002	0,186	0,083	0,271
Photo.jpg	0,001	0,558	0,386	0,945
Lena.bmp	0,002	0,28	0,283	0,565
City.png	0,002	0,499	0,302	0,803
Logo.png	0,002	0,276	0,243	0,521
MilkyWay.tiff	0,002	0,301	0,257	0,56
	0,002	0,368	0,275	0,645

4.16 –

	+		+	
Nure.jpg	8,093	6,53	7,843	22,466
Tulips.jpg	7,885	6,35	7,899	22,134
Photo.jpg	18,764	15,643	18,76	53,167
Lena.bmp	2,485	2,038	2,451	6,974
City.png	9,947	8,293	9,868	28,108
Logo.png	2,389	1,97	2,375	6,734
MilkyWay.tiff	3,166	2,677	3,12	8,963
	7,533	6,214	7,474	21,221

4.17 –

	+		+	
Nure.jpg	29,448	0,206	12,254	41,908
Tulips.jpg	29,6	0,19	12,345	42,135
Photo.jpg	71,225	0,455	29,943	101,623
Lena.bmp	10,204	0,056	4,137	14,397
City.png	38,178	0,336	15,069	53,583
Logo.png	8,882	0,094	3,696	12,672
MilkyWay.tiff	11,834	0,096	4,951	16,881
	28,481	0,205	11,771	40,457

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Tulips.jpg (0,271

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- Logo.png (6,734 ) Lena.bmp (6,974 )

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